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A Dynamical Study of the Non-Star Forming Translucent Molecular Cloud MBM16: Evidence for Shear Driven Turbulence in the Interstellar Medium

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ABSTRACT

We present the results of a velocity correlation study of the high latitude cloud MBM16 using a fully sampled ^{12}CO map, supplemented by new ^{13}CO data. We find a correlation length of 0.4 pc. This is similar in size to the formaldehyde clumps described in our previous study. We associate this correlated motion with coherent structures within the turbulent flow. Such structures are generated by free shear flows. Their presence in this non-star forming cloud indicates that kinetic energy is being supplied to the internal turbulence by an external shear flow. Such large scale driving over long times is a possible solution to the dissipation problem for molecular cloud turbulence.

Subject headings: ISM – Kinematics and dynamics; ISM Clouds; Turbulence

1. Introduction

Suprathermal linewidths are commonly observed in molecular clouds, whether self-gravitating or not. Both internal and external driving mechanisms have been suggested as the source of these velocities (cf. Norman & Silk 1980; Fleck 1983; Henriksen & Turner 1984; Falgarone & Puget 1986; Scalo 1987; Mouschovias 1987; Myers & Goodman 1988; Falgarone & Phillips 1990; Elmegreen 1990; Passot et al. 1995). Virtually every suggested mechanism for producing the observed linewidths requires mass-motions and/or non-linear wave motions both of which are dissipative (Field 1979; Zweibel & Josafatsson 1983; Ghosh et al. 1994). Recent simulations by MacLow et al. (1998) and Padoan & Nordlund (1998) find that MHD turbulence decays on shorter timescales than previously thought. Thus, interstellar turbulence requires continuous injection of kinetic energy. The most obvious source in large clouds is internal star formation. There is, however, a type of molecular cloud, the high latitude translucent variety (van Dishoeck et al. 1991), that show the same superthermal velocity fields but do not display evidence of star forming activity (e.g. Magnani et al. 1995). In the absence of internal driving mechanisms such as star formation or gravity, the motion must be continually produced by an *external* agent.

It is for this reason that we have carried out a dynamical study of the translucent molecular cloud MBM16 (Magnani, Blitz, & Mundy 1985, hereafter referred to as MBM). Our choice of this cloud is quite deliberate. In our earlier paper (Magnani, LaRosa, & Shore 1993, hereafter referred to as MLS93) we reported finding several large-scale formaldehyde clumps in MBM16. These observations in H_2CO indicate that the clumps have a higher density than the rest of the cloud. We concluded that MBM16 is not self-gravitating and that its internal structures are transient. Each clump has a distinct average centroid velocity that differs from the others by about 0.5 km s^{-1} . The difference is not due to a large scale systematic motion. To quantify this, we have examined the standard statistical measures for the line profiles. The velocity centroid dispersion within each clump, $\sigma_c(H_2CO)$ in the notation of Kleiner and Dickman (1985, and references therein) was found to be quite low, $<0.2 \text{ km s}^{-1}$, relative to the cloud as a whole determined from ^{12}CO data, 0.44 km s^{-1} , and relative to the clump to clump centroid velocity difference of 0.5 km/s . The CO data were, however, based on a severely undersampled map. In this study, we present the results of a more extensive ^{12}CO map of the cloud supplemented by new ^{13}CO observations of the densest formaldehyde clump that support and extend our earlier conclusions.

2. Observations

A complete map of MBM16 was made in the ^{12}CO (J=1-0) transition using the 1.2 m Harvard-Smithsonian Center for Astrophysics Millimeter Wave Telescope. The telescope front end configuration is described by Dame (1995). The map is a $6^\circ \times 6^\circ$ grid in Galactic longitude and latitude ($\ell = 168^\circ$ to 174° and $b = -34^\circ$ to -40°) approximately centered on the cloud. The beamwidth of the telescope at 115 GHz is 8.4 arcmin and the separation between the samples was 3.6 arcmin for a total of 97×97 points or 9409 spectra. At the assumed cloud distance of 80 pc (Hobbs et al. 1988) 8.4 arcmin corresponds to a linear resolution of 0.2 pc. The data were taken in frequency-switched mode at a velocity resolution of 0.65 km s^{-1} . The total bandwidth was 150 km s^{-1} centered at 0 km s^{-1} with respect to the LSR. Typical rms noise values for each spectrum were in the 0.133 to 0.281 K range.

A contour map of the integrated antenna temperature ($\int T_A^* dv$) is shown in Figure 1. The velocity map is shown in Figure 2. MBM 16 is clearly centered in the map, and is completely enclosed by the mapping pattern. The general shape of the cloud is similar to the poorly-sampled map by MBM, and the ragged structure is reminiscent of other high latitude clouds. At the bottom left of the field in Figure 1 is a heretofore unidentified high latitude cloud. Since the LSR velocity of the new cloud is significantly different from that of MBM 16, it is likely that the two clouds are at different distances. The molecular gas comprising MBM 16 ranges in velocity from 4 to 10 km s^{-1} , while the new cloud LSR velocities lie between -20 and -5 km s^{-1} . Similarly, in the northeast corner of Figure 1 is a molecular feature which has LSR velocities in the $12\text{-}14 \text{ km s}^{-1}$ range. CO channel maps of this region indicate that this feature is also likely to be a separate molecular cloud (Magnani et al. 1998, in preparation).

We have also mapped the largest formaldehyde clump and a portion of another in ^{13}CO at higher resolution than we reported in MLS93. These data were obtained during two observing sessions at the NRAO⁴ 12 meter telescope at Kitt Peak, Arizona, 1992 Dec. 26 - 1993 Jan. 1 and 1993 July 2 - 7. The 3 mm receiver with an SIS mixer operated with a total system plus sky temperature between 300 and 700 K. Dual polarizations were fed into a 100 kHz filter back end, providing a velocity resolution of 0.26 km s^{-1} . The data were obtained in frequency switched mode with separation of $\pm 2 \text{ MHz}$. The polarizations were averaged together and the resulting spectrum was folded resulting in typical *rms* noise temperatures from 10 to 30 mK after Hann smoothing. We used a uniformly spaced 20×27 grid with 3 arcmin separation

⁴The National Radio Astronomy Observatory is operated by Associated Universities, Inc. in a cooperative agreement with the National Science Foundation.

between beam centers (the beam size is ~ 1 arcmin at 113 GHz). The map concentrated primarily on clump 3 in the H₂CO study described in MLS93, although a portion of clump 2 was included in the western section of the map. The integrated ¹³CO(J=1-0) intensity map of the region is shown in Figure 3. Line emission was detected in about 200 of the 540 map positions.

3. Statistical and Correlation Analyses

For fully developed turbulence, over a large enough region the dispersion in the centroid velocities should be about the same as the individual line widths. The ¹³CO data agrees with the H₂CO results in showing a much smaller centroid dispersion within the clumps. Following Kleiner & Dickman (1985), for the entire sampled cloud the parent velocity dispersion of the mapped region, σ_p (*i.e.*, the average dispersion of the individual spectra, σ_i , is 0.25 km s⁻¹, and the dispersion in the intensity weighted velocity centroids determined from Gaussian profile fitting, σ_c , is 0.31 km s⁻¹. For the leftmost clump located at $\Delta\text{RA} \geq 50.25$) in Fig. 3, $\sigma_i = 0.21$ and $\sigma_c = 0.10$ km s⁻¹. The implication is that the clumps are coherent in velocity. The ¹³CO map is, however, too small to be useful for a correlation study. Our new ¹²CO map is fully sampled and sufficiently large to permit such an analysis.

The velocity correlation function is the simplest description of the dynamical properties of a flow. By definition, the spatial velocity correlation function for a homogeneous turbulent flow is:

$$c_{ii}(\tau) = \langle [v_i(r) - \langle v_i(r) \rangle][v_i(r + \tau) - \langle v_i(r) \rangle] \rangle \quad (1)$$

where the angle brackets denote the spatial averages. The lag, τ , is a scalar quantity. We are, of course, limited to measuring only the radial velocities so we can construct only the longitudinal velocity autocorrelation along the line of sight, $c_{zz}(\tau)$. We normalize the autocorrelation function by its value at zero lag, $C(\tau) = c_{zz}(\tau)/c_{zz}(0)$. In standard terminology, this is known as the biased autocorrelation function (see Miesch & Bally 1994, hereafter referred to as MB94).

Before performing the autocorrelation analysis, we trimmed the data to remove points in the map with velocities that are clearly in excess of the bulk of the cloud. In this case, we retained all points with a signal to noise ratio of 4.5σ or higher with $4.0 \leq v_{rad} \leq 10.0$ km s⁻¹, the range of velocities found within MBM16.

As discussed in Scalo (1984) and further elaborated in MB94, any correlation analysis requires some filtering of the dataset to remove the large scale trends. Therefore, we have applied two different methods to the MBM16 data. In the first procedure, we subtracted the mean velocity, 7.24 km s⁻¹, from the

trimmed map to form the fluctuation map. In the second procedure we subtracted a smoothed map from the data that was obtained from the trimmed map by taking a running mean filter of preset set size that included only detected points. This is the procedure used by Miesch and Bally. We then carried out the autocorrelation analysis of these filtered ^{12}CO data using two independent methods. The first, which is identical to the one described in MB94, used the two dimensional fast Fourier transform (FFT) in IDL. For comparison, in the second we used the scalar algebraic correlation function.

The results are plotted in Figures 4 and 5. Figure 4*a-c* shows the two dimensional correlation results for (a) the mean subtracted, (b) the 15 point smoothed, and (c) the 30 point smoothed maps. In view of the agreement between the different procedures, and the lack of systematic trends in the velocity, we use method (a) for Figure 5 and the subsequent analysis. In Figure 5, we show the comparison between the scalar (1D) and 2D correlation functions for the mean subtracted map. The two methods agree. There is a detectable correlation up to 5 lags or 18.0 arcmin, which corresponds to a physical length of 0.42 pc^5 . To further understand what the correlation function is measuring, and in particular how to define the correlation length, we performed a series of simulations for which the results are shown in Figure 6. To generate a test random map with the same spatial distribution as the real data, we took the trimmed map, normalized it to unity for all detections, and then multiplied each detected location by a gaussian random number with a unit dispersion. The correlation function for this completely random map is shown in Fig. 6a. Notice that although the velocity is spatially confined to the regions where CO was detected, there is no hint of any spatial structure in the Figure. We then simulated the presence of a coherent structure within this map by setting all velocities in a 10×10 region equal to a constant and, in a series of trials, varied the constant. This creates a coherently moving clump of known size and kinetic energy. The velocity was increased from 0 to 2 km s^{-1} to produce a set of maps that were then run through the same analysis as the real data. What they show is that there are clear limits to the information that can be derived from a correlation analysis, but that the detection of a correlated flow is possible.

For instance, in Figures 6*b-d*, the amplitude of the velocity was increased from 0.5 km s^{-1} to 2.0 km

⁵This is about 2.5 beamwidths. We used the same random maps described below to test the effects of beam size on our derived correlation functions. For example, for a gaussian beamwidth (FWHM) of 4 lags convolved with the random map, the correlation function has its first zero at 2 lags. The same map convolved with our beam size yielded no correlation above 1 lag. Therefore, tests show that the correlation we are reporting here does not arise as an artifact of the sampling.

s^{-1} where the random map has velocities in the range -6.3 to 4.4 km s^{-1} . Again, we note that the velocity dispersion was 1 km s^{-1} . With an amplitude of 0.5 km s^{-1} , the clump had about 3% of the total power in the map, and the structure was clearly undetectable (Fig. 6b). For 1 km s^{-1} , or about 13% of the total power, the structure is obvious (Fig. 6c), and becomes more so with increasing energy. An additional result of the simulations is that the size of the coherent region is not the e^{-1} point but where the correlation function has its first zero (e.g. Townsend 1976). More important is the result that the lack of detection of a coherent region by the correlation method merely places an upper limit on the size and power of such regions, but does not rule out their presence.

4. Discussion

On the basis of a purely statistical analysis of the line profiles for a number of molecular species, ^{12}CO , ^{13}CO , and H_2CO , it is clear that MBM16 contains a number of regions with exceptionally low dispersions in the line centroid velocity. We emphasize that these are not simply “quiet spots” in the flow. The individual profiles throughout these regions have the same widths as the rest of the cloud, which is much larger than the dispersion in the centroids. The implication of this observation is that the size-line width relation (Larson 1981) breaks down for this cloud. This is shown in detail in Figure 7. There is no systematic trend to the data, and those regions identified in MLS93 from the formaldehyde observations clearly stand out in the ^{12}CO data as anomalously underdispersed for their size.

The results of our correlation analysis support and strengthen these statistical conclusions. We find a correlation length of roughly 18 arcmin, corresponding to a physical scale of about 0.4 pc. Our simulations suggest that these regions must together contain at least 10% of the kinetic energy of the cloud. We argue that these regions are the interstellar analogs of the *coherent structures* that usually accompany turbulence generated in free and bounded shear flows. These have been the subject of increasing attention in the past few years as their importance in turbulence has been more clearly recognized in terrestrial flows (e.g. Lumley 1989; George & Arendt 1991; Robinson 1991; McComb 1991; Shore 1992; Holmes, Lumley, & Berkooz 1996).

In the most general case where the flow can be driven both internally and externally, it is likely that no single source scale would be detected using correlation methods because none exists. Instead, the variety of processes act on so many different scales that the no one produces a clean dynamical signature. As far we

know, there have been no previous dynamical studies of any *isolated* non-star forming cloud⁶. It is therefore not surprising that no unambiguous velocity correlation length is generally found (e.g. MB94). Scalo (1984) suggested that a length scale of order 0.3 pc in the ρ Oph cloud might be due to turbulence, although it was possible that large scale structure could produce a similar signature. It is precisely the simplicity of the velocity field in MBM16 that makes such a detection more likely if it exists. This cloud is nearby so we can obtain fully sampled maps of comparatively small scale structures. More important, the lack of internal sources for turbulence in MBM16 means that any external driver will leave a recognizable signature in the velocity field of the cloud.

If we are correct in assigning the source of the coherent structures to an external shear flow, then there are important consequences for the interpretation of the line profiles in this and other clouds. First, such phenomena should be ubiquitous in the interstellar medium. For instance, any H I cloud should show similar structures. Boundary layer effects have already been invoked in chemical studies of molecular clouds (e.g. Charnley et al. 1990). In particular, we suggest that a correlation analysis of a high velocity H I cloud might reveal coherent structures generated by boundary shear with the interstellar medium⁷. Second, such driven turbulence will produce MHD waves so long as the fluid and magnetic field are coupled. This is true throughout the interstellar medium. Third, the fact that large scale external driving can feed the observed internal motions points to a long-lived source. Even though both MHD waves and turbulence are intrinsically dissipative, the longevity of the driver can overcome the dissipation and maintain the stability of the clouds for very long times. Thus, the detection of turbulence does not imply any particular youth for the clouds.

5. Summary

Our purpose in this paper has been to characterize the velocity field within a non-star forming molecular cloud. We were guided by earlier H₂CO observations at 6 arcmin resolution (0.14 pc) that showed dynamical ordering on a length scale of about 0.5 pc. Using higher resolution and a far more complete ¹²CO

⁶Although Heiles 2 and other non-star forming clouds have been observed, these are all associated with or imbedded within larger star forming cloud complexes. MBM16 is completely isolated.

⁷Recent analytic and numerical work by Vietri, Ferrara, & Miniati (1997) suggests that non-self gravitating clouds are not disrupted by the Kelvin-Helmholtz instability.

map, we find evidence for a velocity correlation on a scale of 0.4 pc. We attribute this to the formation of coherent structures in an externally driven turbulent shear flow. This could easily be the source for both MHD and fluid turbulence on small scale within this and other molecular clouds⁸ and supply kinetic energy to the clouds on potentially long timescales.

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⁸This explanation may specifically apply to giant molecular clouds. For instance, Williams, Blitz, & Stark (1995) have observed numerous clumped structures in turbulent clouds that do not contain embedded stars yet otherwise display the same turbulence properties as we have discussed here. We thank the referee, T. Harquist, for suggesting this addition.

Figure captions

Fig. 1. ^{12}CO J=1-0 contour map of a $6^\circ \times 6^\circ$ region centered on MBM16. The velocity range of the map is $-10 \leq v_{\text{LSR}} \leq 15 \text{ km s}^{-1}$. The contours are at [10, 30, 50, 70, 80, 90, 95] percent of the maximum CO intensity of 7.23 K km s^{-1} . The objects to the extreme northeast and southeast of the map are probably not associated with MBM16 (see text). The size of the 8.4 arcmin beam, the effective map resolution, is shown in the upper right corner.

Fig. 2. ^{12}CO velocity map corresponding to the cloud shown in Fig. 1. This map corresponds to the velocity range 4 to 10 km s^{-1} . The orientation is the same as Fig. 1. One lag corresponds to 3.6 arcmin for the fully sampled map.

Fig. 3. The ^{13}CO (J=1-0) velocity map of a subregion in MBM16. The (0,0) location corresponds to $(\alpha, \delta) = (3^h 21^m 48^s, 10^\circ 42' 00'')$ in 1950 coordinates. The region covered by the map encompasses all of clump 3 and the eastern portion of clump 2 as defined in MLS93. The sampling is every $3'$ with a $1'$ beam and surface plot shows all velocities greater than 5 km s^{-1} (maximum is 8 km s^{-1}).

Fig. 4. Two dimensional velocity correlation function for different normalizations (see text) obtained by (a) subtracting a constant mean for the cloud of 7.24 km s^{-1} ; (b) subtracting a smoothed map with a 15 point running mean; and (c) subtracting a 30 point running mean.

Fig. 5. Comparison of the one and two dimensional velocity correlation functions for the mean subtracted data. Note that the scalar correlation function, the solid line in the figure, is *not* a fit to the points.

Fig. 6. Results of simulations of a coherent structure in a normally distributed velocity fluctuation map. The figure shows the 2D velocity correlation function for simulations described in the text with (a) $\Delta v = 0 \text{ km s}^{-1}$; (b) 0.5 km s^{-1} ; 1.0 km s^{-1} ; (d) 2 km s^{-1} .

Fig. 7. Size-line width results for the ^{12}CO data for MBM16. The squares represent the H_2CO clumps

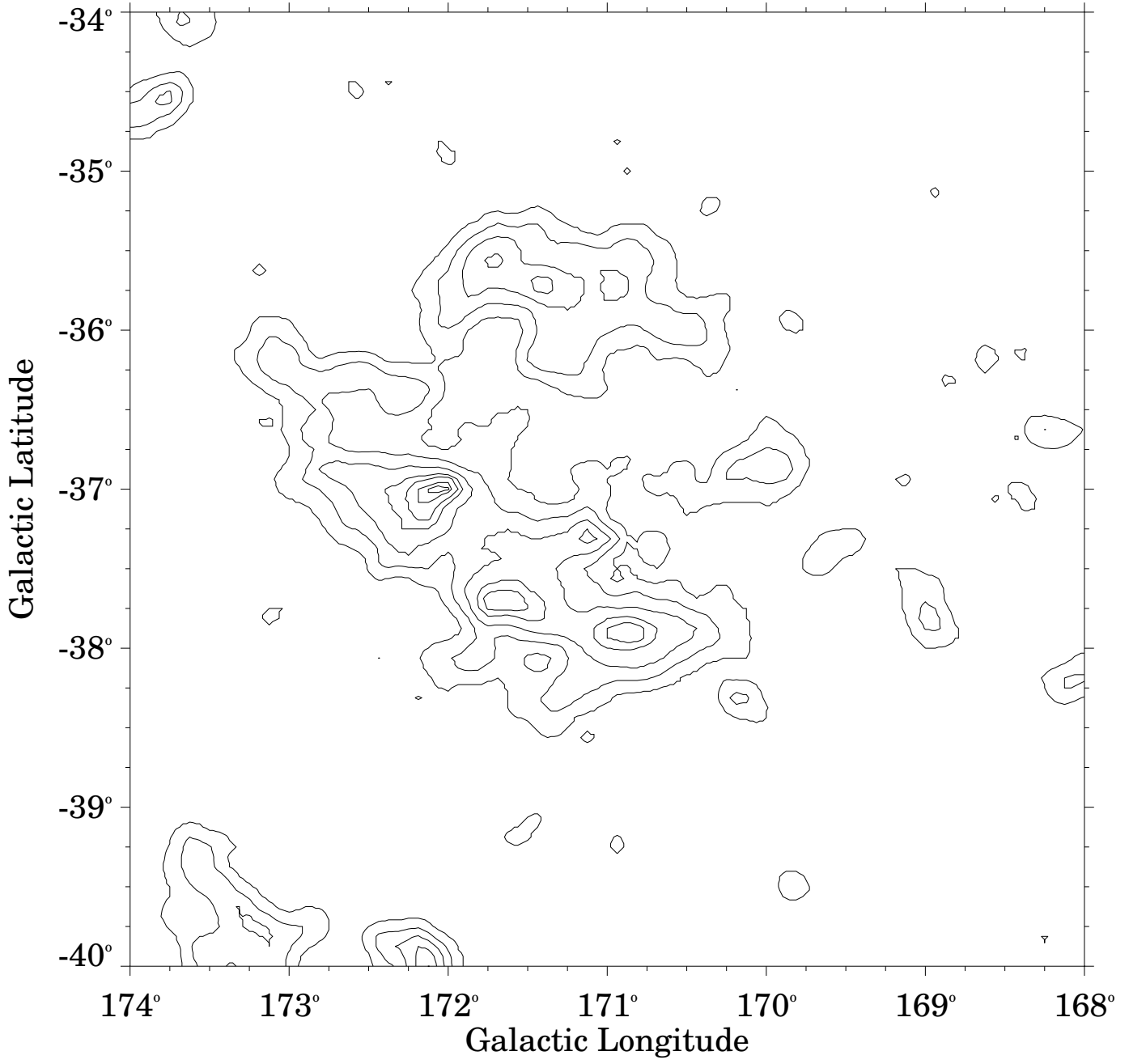
while the crosses are for regions throughout the cloud. The length scale is the square root of the number of detected points within the sampled region. The centroid velocity dispersion was determined from the intensity weighted centroids of the individual line profiles. Notice the distinct separation of the clumps from the bulk of the data and the absence of any obvious overall trend.

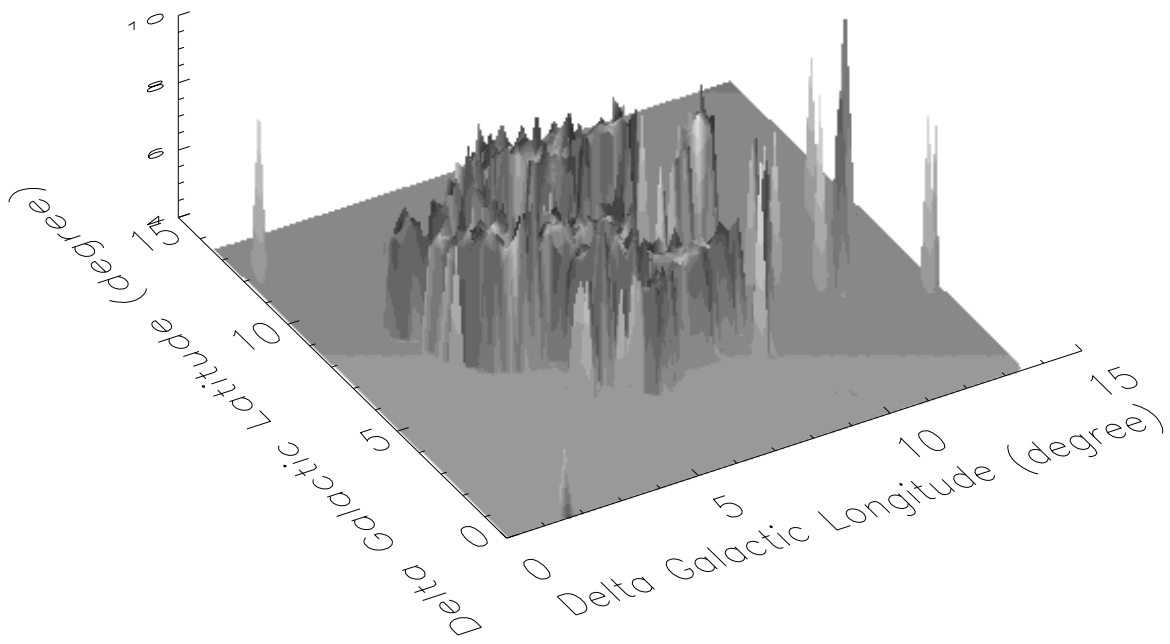
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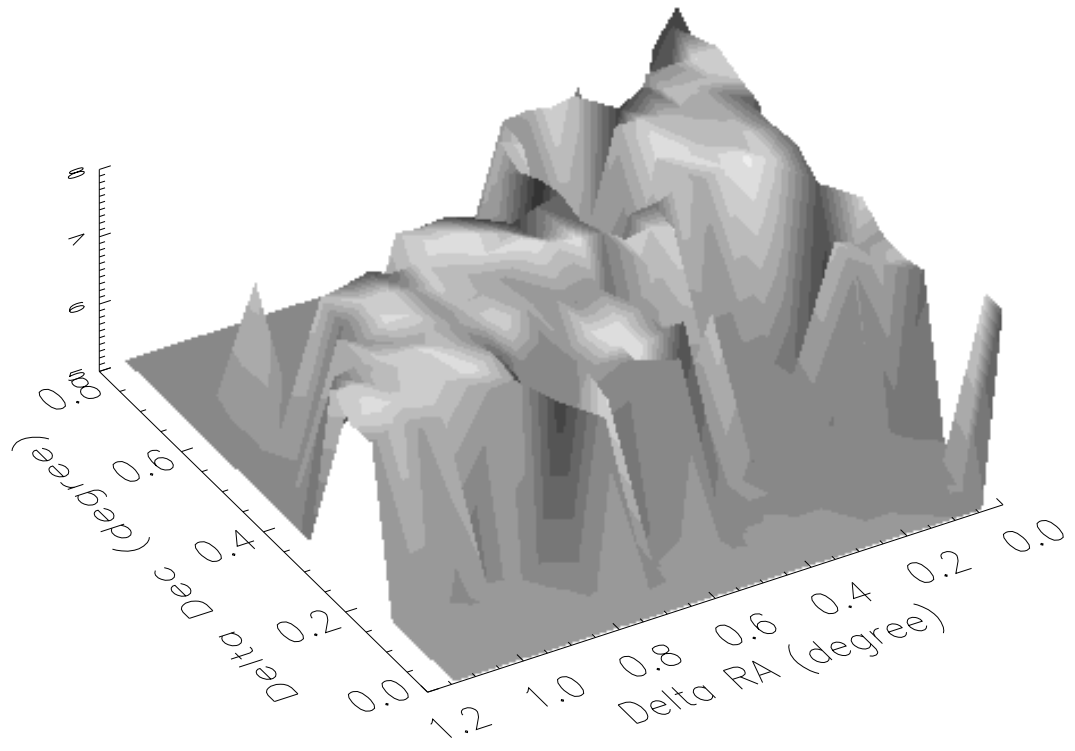
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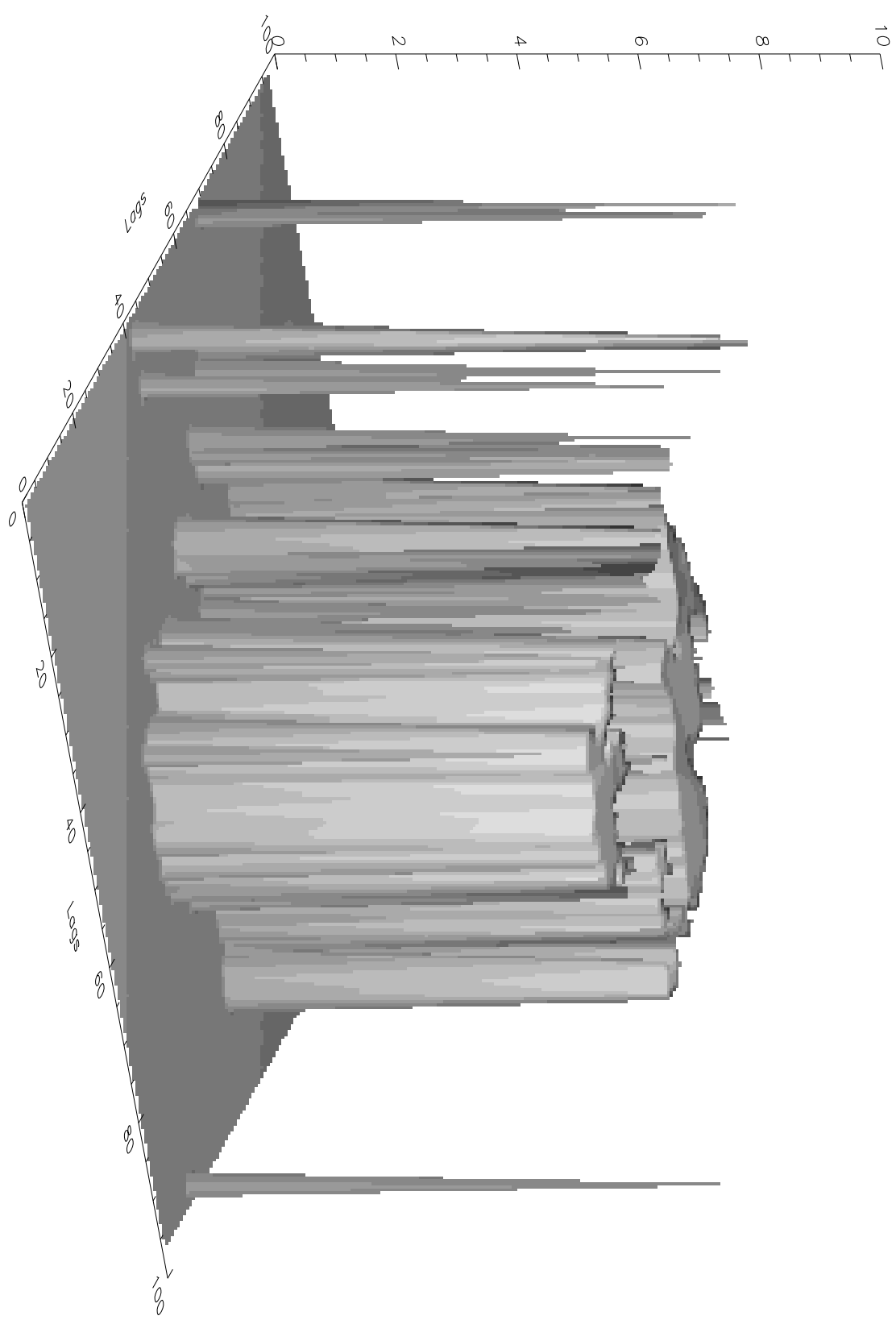
MBM16; $V_{\text{LSR}} = [-20, +15] \text{ km s}^{-1}$

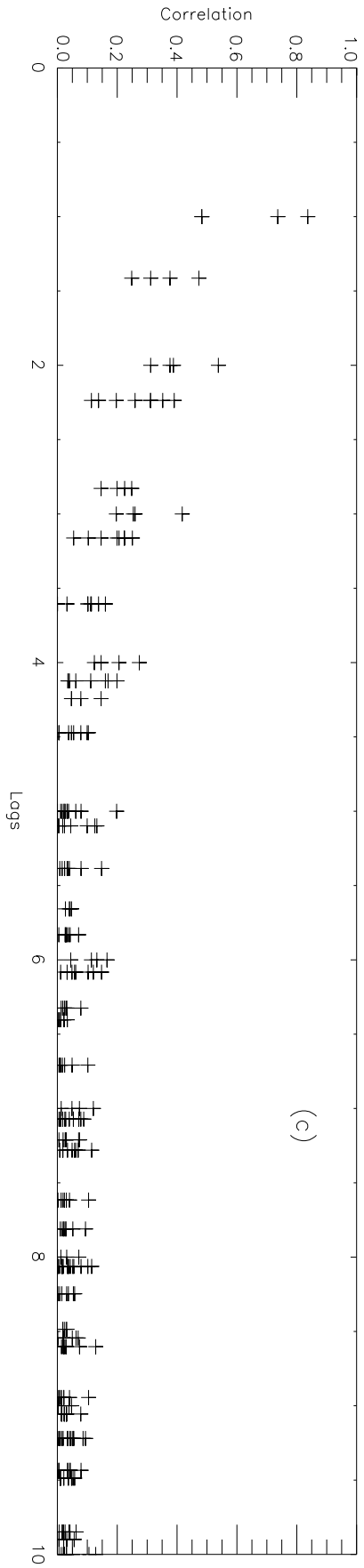
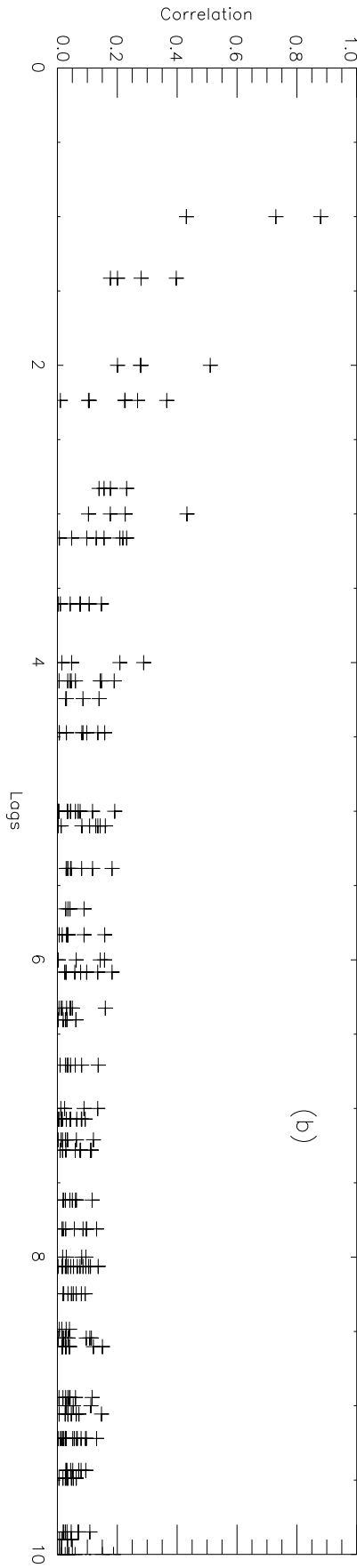
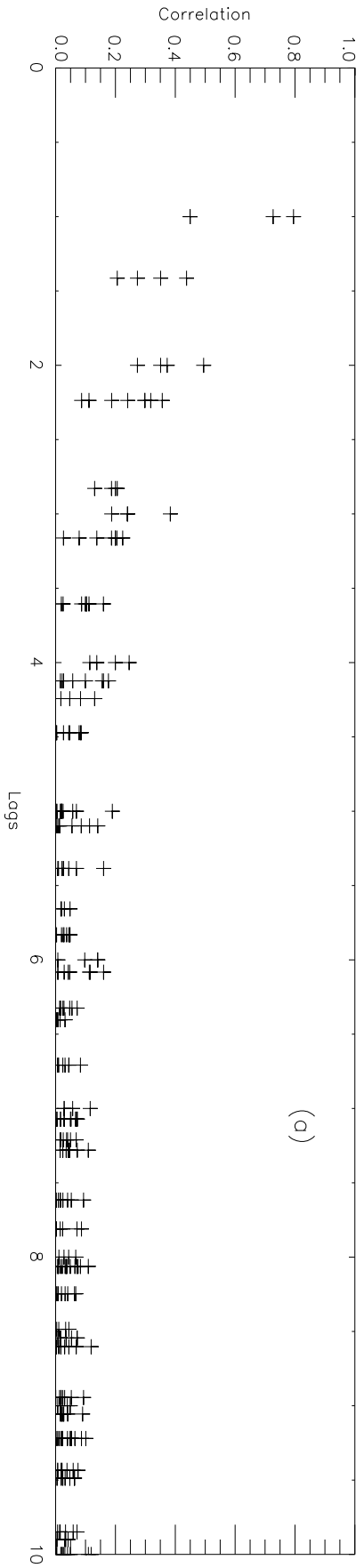


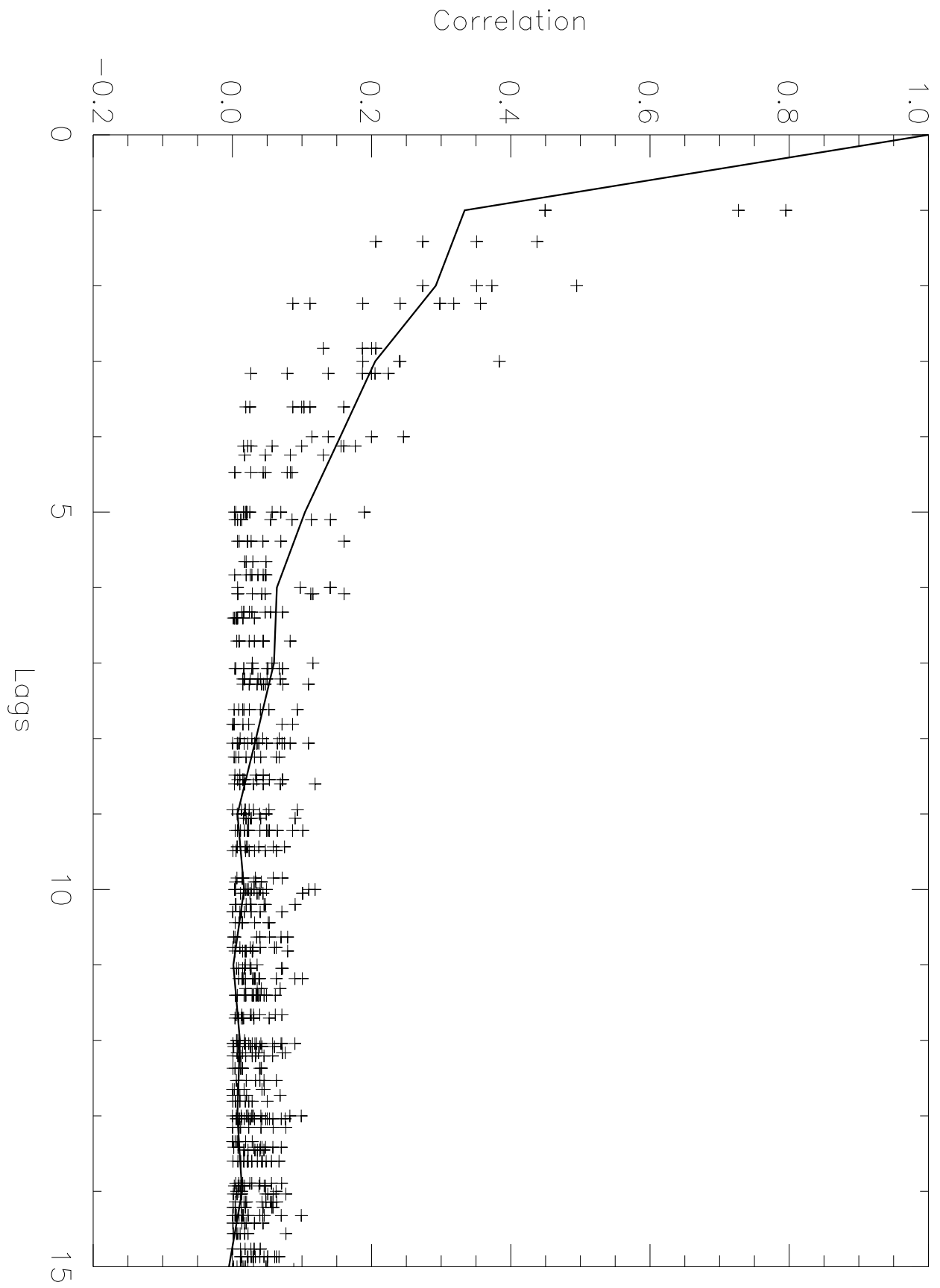


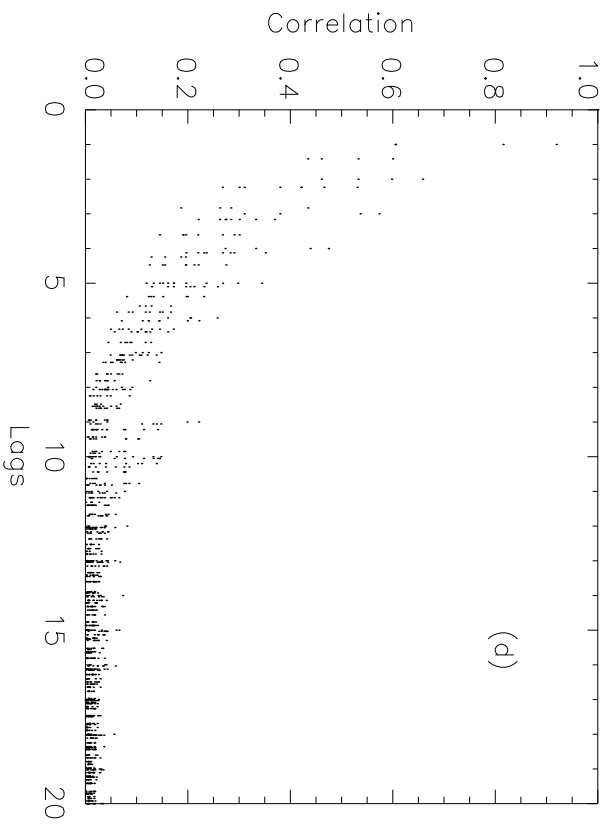
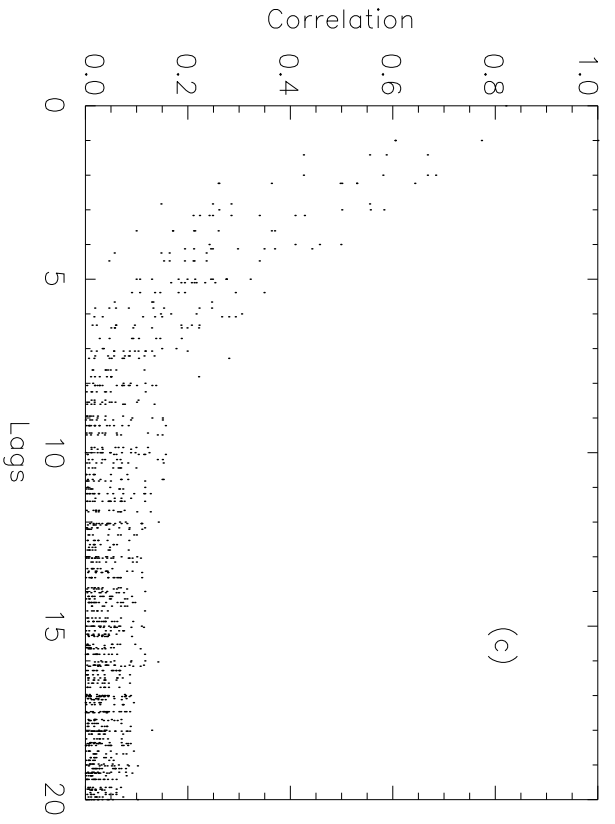
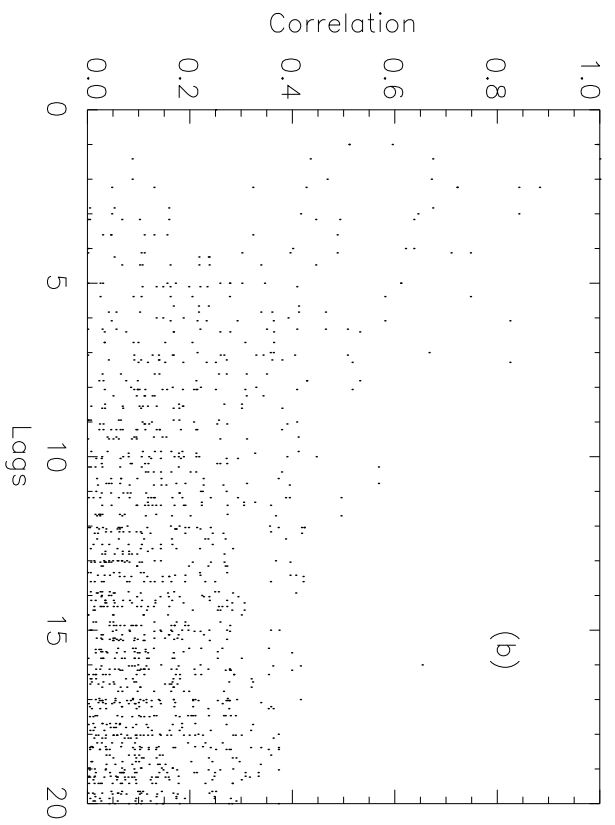
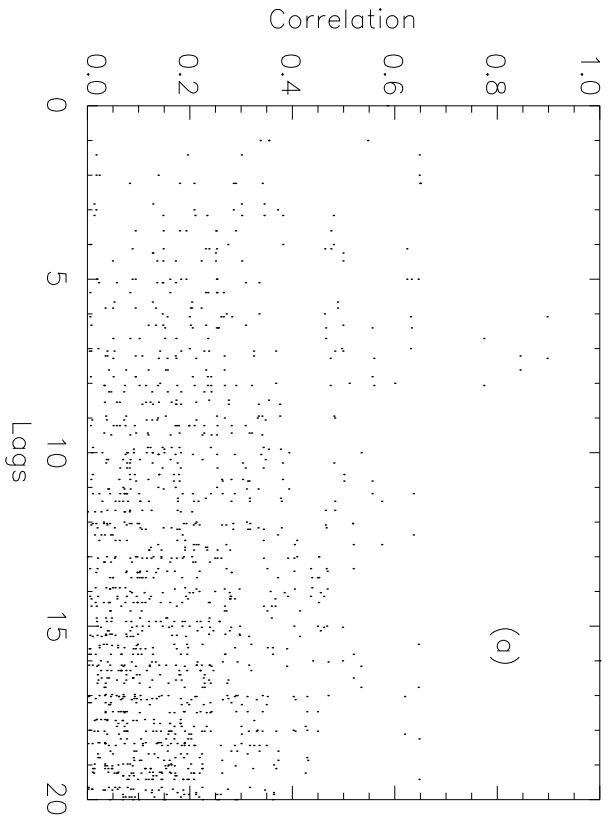


Variable smoothing, trimmed data, 15 pt









Centroid Velocity Dispersion

